# Two-Dimensional Structures of Crystalline Self-Aggregates of Amphiphilic Alcohols at the Air-Water Interface As Studied by Grazing Incidence Synchrotron X-ray Diffraction and Lattice Energy Calculations ${ }^{8}$ 

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#### Abstract

The two-dimensional (2D) crystal structures of self-aggregated clusters of amphiphilic alcohols $\left(\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}\right.$, $n=23,30,31$, and $\mathrm{C}_{19} \mathrm{H}_{3} \mathrm{CO}_{2}\left(\mathrm{CH}_{2}\right)_{n} \mathrm{OH}, n=9,10$ ) on pure water at a temperature of $5^{\circ} \mathrm{C}$ have been determined to near-atomic resolution in order to understand the relative abilities of these monolayers to induce ice nucleation. The structures were solved making use of grazing incidence synchrotron X-ray diffraction (GID) data, complemented by lattice energy calculations. The GID data of the different monolayers within each of the two series $\left(\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}\right.$, $\mathrm{C}_{19} \mathrm{H}_{39} \mathrm{CO}_{2} \mathrm{C}_{n} \mathrm{H}_{2 n} \mathrm{OH}$ ) are very similar. The molecules pack in a rectangular unit cell of average dimensions $a=5.0$ $\AA, b=7.5 \AA$ for the normal alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$ and $a=5.7 \AA, b=7.5 \AA$ for $\mathrm{C}_{19} \mathrm{H}_{39} \mathrm{CO}_{2} \mathrm{C}_{n} \mathrm{H}_{2 n} \mathrm{OH}$. The plane group symmetry is essentially $p 1 \mathrm{~g} 1$ for the normal alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$ and essentially $p 11 \mathrm{~g}$ for the other group. The molecular chains are tilted from the vertical by an average angle of $9^{\circ}$, in the direction of the $b$ axis, for $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$ and by $29^{\circ}$, in the direction of the $a$ axis, for the other molecular type. The molecular chains related by glide ( $g$ ) symmetry are arranged in a herringbone pattern. The fit to the Bragg rod intensity data of $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$ permitted a reliable estimate of $0.07 \AA^{2}$ for the molecular mean-squared motion parallel to the water surface. The absolute orientations of the molecules $\mathrm{C}_{19} \mathrm{H}_{39} \mathrm{CO}_{2} \mathrm{C}_{\mathrm{n}} \mathrm{H}_{2 n} \mathrm{OH}$ were determined by lattice energy calculations. The anisotropic coherence lengths of the crystallites of $\mathrm{C}_{19} \mathrm{H}_{39} \mathrm{CO}_{2} \mathrm{C}_{n} \mathrm{H}_{2 n} \mathrm{OH}$ derived from the widths of the two observed Bragg peaks have been correlated with the binding energies of molecules in different directions.


## 1. Introduction

Recently we demonstrated that amphiphilic long-chain alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$ arranged in monolayers at the surface of water drops have the ability to promote ice nucleation. ${ }^{1}$ The temperature of freezing of these water drops was found to be dependent upon both the length of the hydrocarbon chain and the parity of $n$, the number of carbon atoms in the chain. For the odd series, the freezing temperature rose from -11 to $0^{\circ} \mathrm{C}$ on increasing the chain length from $n=17$ to 31 ; for the even series the freezing point leveled off at a temperature of $-8^{\circ} \mathrm{C}$, with $n$ in the range $22-30$. The ice-nucleating effect was accounted for by an assumed spontaneous formation of ordered two-dimensional (2D) clusters of alcohol molecules at the water surface, ${ }^{1}$ with lattice dimensions close to those of the $a b$ lattice of hexagonal ice. It was therefore deemed necessary to obtain direct information on the molecular packing of these amphiphiles to test this proposed mechanism.

In a previous paper ${ }^{2}$ we reported results of a general nature on grazing incidence $X$-ray diffraction (GID) measurements using synchrotron radiation on uncompressed monolayers of three alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$, with different chain lengths and parities ( $n$ $=23,30,31$ ) over water at $5^{\circ} \mathrm{C}$. The measurements, described here in part 6.1, indicated a high degree of lateral crystalline order for all three monolayers. The coherence lengths ${ }^{3} L$ of the 2D crystallites of the monotayers were anisotropic in the range 250 and $1000 \AA$.

[^0]The measured GID patterns for the three alcohol monolayers ( $n=23,30,31$ ) were similar but for minor differences in peak positions. The Bragg peaks for the three monolayers are shown in Figure 1. The three observed Bragg reflections for each monolayer were indexed as $\{1,1\}+\{1, \overline{1}\},\{0,2\}$, and $\{2,0\}$ for a rectangular cell, ${ }^{2}$ and the resulting unit cell parameters are listed in Table 1. The positions of the maxima of the Bragg rod intensity profiles of the three reflections indicated that the molecular axis lies approximately in a plane perpendicular to the short $a$ axis of the unit cell, with an average tilt angle of $9^{\circ}$ from the surface normal (Table 1).

The packing arrangements of the hydrocarbon chains were deduced from the 3D crystal structures of long-chain alcohols and alkanes. Such molecules adopt a layer structure, ${ }^{4-6}$ in which neighboring hydrocarbon chains are related by glide symmetry, forming a herringbone arrangement, generally specified as the orthorhombic orthogonal $\left(\mathrm{O}_{\perp}\right)$ motif. ${ }^{4.6}$ The dimensions of the cell perpendicular to the molecular axis are 4.98 by $7.42 \AA$. The dimensions of the unit cell for the alcohol monolayers projected along the molecular chain axis (Table 1) match well with those of the orthorhombic subcell of the 3D crystal structures. Thus we proposed ${ }^{2}$ that in the monolayer crystallites of $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$ ( $n=23,30,31$ ) the chains pack in a primitive rectangular cell in which the molecules are tilted in the $b$ direction and related to each other by a glide perpendicular to the $a$ axis, in the symmetry plane group plgi.

[^1]

Figure 1. Observed Bragg diffraction peaks for $\{1,1\}+\{1, \overline{1}\},\{0,2\}$, and $\{2,0\}$ reflections across the horizontal scattering vector $\mathbf{q}_{x y}$ for the alcohol monolayers ( $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}, n=23,30,31$ ).

Table 1. Results ${ }^{a}$ of Bragg Peak Analysis for the Alcohol Monolayers $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}, n=23,30,31$

|  | $d_{11}, d_{11}$ <br> $(\AA) L(\AA)$ | $d_{02}(\AA)$ <br> $\mathrm{L}(\AA)$ | $d_{20}(\AA)$ <br> $\mathrm{L}(\AA)$ | $a(\AA)$ <br> $\left(a_{\mathrm{p}}\right)$ | $b(\AA)$ <br> $\left(b_{\mathrm{p}}\right)$ | $A$ <br> $\left(\AA^{2}\right)$ | $t$ <br> $(\mathrm{deg})$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $n=23$ | 4.18 | 3.78 | 2.50 | 5.00 | 7.56 | 18.90 | 9.5 |
|  | $\geq 1000$ | 360 | $\geq 1000$ | $(5.00)$ | $(7.46)$ |  |  |
| $n=30$ | 4.15 | 3.75 | 2.49 | 4.99 | 7.49 | 18.69 | 7.7 |
|  | $\geq 1000$ | 230 | $\geq 1000$ | $(4.99)$ | $(7.42)$ |  |  |
| $n=31$ | 4.16 | 3.77 | 2.49 | 4.99 | 7.53 | 18.79 | 10.1 |
|  | $\geq 1000$ | 270 | 700 | $(4.99)$ | $(7.41)$ |  |  |

$a_{t}=$ tilt angle of monolayer molecules from the normal to the water surface. $L=$ coherence length ( $\AA$ ) of the crystallites, determined using the Scherrer formula. ${ }^{3} a$ and $b$ are the lengths of the unit cell axes; $a_{\mathrm{p}}$ and $b_{\mathrm{p}}$ are the lengths of the unit cell projected along the molecular chain axis. In these systems, $a_{\mathrm{p}}=a$ and $b_{\mathrm{p}}=b \cos t$. $A=$ area per molecule $=a b / 2$.

In order to obtain a more definitive picture of the molecular packing of the alcohol monolayers at the air-water interface, we adopted a procedure described in a preceding paper ${ }^{7}$ for pinpointing 2D crystal structures, involving an analysis of the Bragg rods complemented by lattice energy computations of a variety of possible packing arrangements.

We were faced with the question not only as to the precise packing of the alcohol chains in the 2D crystals of $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$ ( $n=23,30,31$ ) but also as to the conformation of their hydroxyl head groups. Indeed the GID data from 2D crystallites is not sufficiently sensitive to minor differences in molecular conformation at the head-group level. According to IR spectroscopy and X-ray diffraction data, the 3D crystals of the normal higher alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}(n>15)$ appear in either the $\gamma$ or $\beta$ forms. ${ }^{8-10}$ In the $\gamma$ form, all the alcohol chains adopt an all-trans conformation. They are tilted at an angle of approximately $35^{\circ}$ from the axis perpendicular to the crystal layer and are arranged in the orthogonal $\left(\mathrm{O}_{\perp}\right)$ motif. The molecular chains in the $\beta$ form are almost perpendicular to the crystal layer, as indicated by the crystal structure of 1-heptanedecanol ${ }^{8,11}\left(\mathrm{C}_{17} \mathrm{H}_{35} \mathrm{OH}\right)$, and are also arranged in the orthogonal $\left(\mathrm{O}_{\perp}\right)$ motif. In contrast to the case of the $\gamma$ form, the conformation of the terminal $\mathrm{C}_{\alpha}-\mathrm{OH}$ group is gauche about the $\mathrm{C}_{\beta}-\mathrm{C}_{\alpha}$ bond for half the number of molecules and trans for the other half. Theoretical studies
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(11) ONly the cell parameters and a figure of the crystal structure of 1-heptadecanol have been published ${ }^{8}$ but without atomic coordinates.
examining the interface between a hexanol monolayer and water predict that an average of two water molecules form hydrogen bonds with each hexanol molecule. ${ }^{12}$ They also indicate that the terminal $\mathrm{C}-\mathrm{OH}$ bond of the $\mathrm{C}-\mathrm{C}-\mathrm{C}-\mathrm{OH}$ moiety can be in a trans or gauche conformation with equal probability. Thus we performed X-ray diffraction measurements on single 3D crystals of the following alcohols, $\mathrm{HO}\left(\mathrm{CH}_{2}\right)_{9} \mathrm{OH}, \mathrm{HO}\left(\mathrm{CH}_{2}\right)_{10} \mathrm{OH}, \mathrm{C}_{24} \mathrm{H}_{49^{-}}$ OH , and $\mathrm{C}_{25} \mathrm{H}_{51} \mathrm{OH}$, in order to extract more information on the conformation of the terminal head group, as described in parts 6.2 and 6.3.

The freezing point studies on water drops covered with monolayers were extended, as described in an accompanying paper, ${ }^{13}$ making use of alcohols with functional groups such as secondary amide ( CONH ) or carboxy ester $\left(\mathrm{CO}_{2}\right)$ groups inserted in the chain to help induce packing arrangements different from those of the normal alcohols.
Monolayers of hydroxy alkyl esters of eicosanoic acid $\mathrm{C}_{19} \mathrm{H}_{39}-$ $\mathrm{CO}_{2}\left(\mathrm{CH}_{2}\right)_{n} \mathrm{OH}, n=9,10$, were found to induce ice nucleation ${ }^{13}$ although not as effectively as the normal long-chain alcohols. The monolayers of the hydroxy alkyl esters with $n=10$ induce ice nucleation at a higher temperature than those with $n=9$. On the assumption that the molecular chains are strongly tilted to the normal of the water surface, these results suggested that the difference in ice-nucleating temperature may be associated with a difference in alcohol OH orientation with respect to the water surface, provided the absolute orientation of the molecular chain is the same for the two molecules $\mathrm{C}_{19} \mathrm{H}_{39} \mathrm{CO}_{2}\left(\mathrm{CH}_{2}\right)_{n} \mathrm{OH}, n=9$, 10. The presence of the carboxy group $\left(\mathrm{CO}_{2}\right)$ in the molecular chain should allow us to fix the orientation of the molecule and so that of the OH head group with respect to the water surface. Thus we also performed GID measurements using synchrotron X-radiation on 9-hydroxynonyl eicosanoate (HNE, $\mathrm{C}_{19} \mathrm{H}_{39}$ $\mathrm{CO}_{2}\left(\mathrm{CH}_{2}\right)_{9} \mathrm{OH}$ ) and 10-hydroxydecyl eicosanoate (HDE, $\mathrm{C}_{19} \mathrm{H}_{39}$ $\left.\mathrm{CO}_{2}\left(\mathrm{CH}_{2}\right)_{10} \mathrm{OH}\right)$, as described in part 6.1.

## 2. Methodology of 2D Structure Determination

Here we describe the methodology adopted to determine the 2D crystal structures of the alcohol monolayers making use of the GID data and lattice energy calculations. ${ }^{7}$

The Bragg rod intensity profile can be expressed in terms of the molecular X-ray structure factor as follows

$$
\begin{equation*}
I_{h k}\left(q_{z}\right)=K L P A_{A B C D} A_{\text {cell }}{ }^{-2} V\left(q_{z}\right)\left|F_{h k}\left(q_{z}\right)\right|^{2} D W_{h k}\left(q_{z}\right) \tag{1}
\end{equation*}
$$

The observed Bragg rod intensity is actually a sum over those ( $h, k$ ) reflections whose Bragg rods coincide at a particular horizontal $2 \theta_{h k}$ angle, or $q_{h k}$ position, where $q_{h k}=4 \pi \sin \theta_{h k} / \lambda$. In eq 1 , the most important variation is due to the square of the molecular structure factor $\left|F_{h k}\left(q_{z}\right)\right|^{2}$. The Debye-Waller factor $\mathrm{DW}_{h k}\left(q_{z}\right)=\exp -\left(q_{h k}{ }^{2} U_{x y}+q_{z}{ }^{2} U_{z}\right)$, where $U_{x y}$ and $U_{z}$ are respectively the mean-square amplitudes paraliel and perpendicular to the monolayer plane. They account for the thermal motion of the atoms ${ }^{14,15}$ in the molecule, as well as for ripples on the water surface, which lead to roughness of the interface. ${ }^{16-18}$

[^2]The grazing geometry factor $V\left(q_{z}\right)$ describes the interference between the waves which are diffracted up from the monolayer and those that are diffracted down and subsequently reflected up; ${ }^{19.20}$ it is seen as a sharp peak at $q_{z} \approx 0.01 \AA^{-1}$. The corrections for crossed-beam area $A_{A B C D}$, depicted in the Experimental Section and in Figure $18\left(A \propto 1 / \sin 2 \theta_{h k}\right)$, Lorentz ( $L \propto 1 / \sin 2 \theta_{h k}$ ), and polarization $\left(P=\cos ^{2} 2 \theta_{h k}\right)$ have been inserted; $A_{\text {cell }}$ is the area of the unit cell. The factor $K$ scales the calculated to the observed intensity.

The scarcity of observable Bragg rod data, due in part to the fact that the monolayers at the water surface are composed of a 2D crystalline "powder", ${ }^{21}$ imposed a model with a small number of adjustable parameters. Thus we have refined the alcohol chain as a rigid body with one positional parameter (translation along the $x$ or $y$ direction depending upon the crystal symmetry) and three orientational parameters defined by the Eulerian angles $\omega$, $t$, and $\phi{ }^{22.23}$ The various model structures were each refined and eventually compared by the fitting of their calculated Bragg rod intensity profiles to the observed measurements. Molecular models on the atomic scale of the alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}(n=23$, 30,31 ) were constructed making use of low-temperature 3D singlecrystal structures of normal aliphatic alcohols and diols, presented in this paper (see parts 6.2 and 6.3). The crystal structure of the diol $\mathrm{HO}\left(\mathrm{CH}_{2}\right)_{9} \mathrm{OH}$ was used to construct the gauche conformation adopted by the $\mathrm{C}_{\alpha}-\mathrm{OH}$ group. The carbon skeleton of the alltrans chain was assumed to be coplanar.

The molecules of $\mathrm{C}_{19} \mathrm{H}_{39} \mathrm{CO}_{2} \mathrm{C}_{n} \mathrm{H}_{2 n} \mathrm{OH}, n=9,10$, namely HNE and HDE, were assumed to adopt an all-trans conformation for the two hydrocarbon segments, in accordance with the 3D crystal structure of ethyl stearate. ${ }^{24}$ The geometry of the ester moiety was taken from the crystal structures of 4-oxo-2-butenoic acid alkyl esters. ${ }^{25}$ The conformation of the ester segment $\mathrm{C}-\mathrm{C}$ -$\mathrm{CO}-\mathrm{O}-\mathrm{C}$ was assumed to be all-trans in accordance with observation. ${ }^{26}$

Atom-atom potential energy calculations which have proven to be an alternative method for confirmation or indeed ab initio prediction of possible 3D crystal structures, ${ }^{27,28}$ were also applied as a complementary method for the 2D structure elucidation. The van der Waals parameters for each pair of atoms for the lattice energy calculations were taken from the results derived by Lifson, Hagler, and co-workers. ${ }^{28}$ The electrostatic parameters in the form of net charges and dipole and quadrupole moments on each atom for the Coulomb energy calculations were extracted from the electron density deformation distribution derived from a low-temperature X-ray diffraction study of 1,3-diethylbicy-

[^3]clobutane-exo,exo-2,4-dicarboxylic acid. ${ }^{29}$ The parameters pertaining to the atoms of the carboxyl moiety in this compound were used for the corresponding atoms of the carboxy ester moiety $\mathrm{CO}_{2}$ in the HNE and HDE molecules. Since no analogous data of an alcohol were available, the electrostatic parameters of the alcohol hydroxyl group were derived from the atomic moments of a water molecule from a low-temperature X-ray diffraction study of cytosine monohydrate. ${ }^{30}$

The feasibility of obtained meaningful results in monolayers from such a procedure has already been demonstrated ${ }^{7}$ by a determination of the 2D crystal structure of an uncompressed monolayer of $\mathrm{C}_{29} \mathrm{H}_{59} \mathrm{CO}_{2} \mathrm{H}$ over pure water at a temperature of $5^{\circ} \mathrm{C}$.

## 3. Results on Monolayers of the $\mathrm{C}_{n} \boldsymbol{H}_{2 \mathrm{D}+1} \mathrm{OH}$ Series

3.1. Comparison of the Various Possible 2D Packing Arrangements. We shall first construct possible packing arrangements of the $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$ molecules assuming the planar alltrans conformation of the carbon skeleton and that the molecules pack in a rectangular cell and are tilted by $9^{\circ}$ from the vertical in the direction of the $b$ axis. The feasible 2D plane groups ${ }^{31}$ for a rectangular unit cell are $c 1 m 1, p 2 m g, p 11 g, p 1 g 1$. The plane group $\operatorname{clm} 1$ describes a translational packing in which parallel molecules lie on a mirror plane in a $c$-centered cell (Scheme 1a). The plane group $p 2 m g$ imposes a similar mirror constraint, but the glide plane, which is perpendicular to the mirror plane, induces the molecules to tilt in alternating directions to the mirror plane (Scheme 1 b ). With plane group $p 11 g$ the mirror constraint is dropped but leaves the molecules to tilt in alternating directions (Scheme 1 c ). In the case of plane group $p 1 \mathrm{gl}$, all the molecular chain axes are parallel, but not the planes through the molecules related by glide symmetry (Scheme 1d). There does remain the possibility of an oblique, primitive cell $p 1$, but where the nonsymmetry-related $\{1,0\}$ and $\{0,1\}$ reflections corresponding to the basal reciprocal axes coincide to yield a unit cell in real space, which may be expressed as a $c$-centered rectangular with symmetry $c 1$, as shown in Scheme 1 e .

Employing eq 1, the intensity profiles of the Bragg rods corresponding to the three measured reflections $\{1,1\}+\{1, \overline{1}\}$, $\{0,2\}$, and $\{2,0\}$ of each of the three 2D crystalline powders were calculated using atomic coordinate models of the $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$ ( $n$ $=23,30,31$ ) molecules. So as to generate all possible 2D crystal structures with plane symmetries $p 11 g$ and $p 2 m g$ (which is a special case of $p 11 \mathrm{~g}$ ), the molecules were given full rotation about their long axes and translated along the $b$ axis from $y=-0.25$ to +0.25 (the glide plane is at $y= \pm 0.25$ ). ${ }^{32}$ The ratio of the calculated intensities of the two reflections $I_{\{0,1\}}: I_{\{1,1\}+\{1, \mathrm{i}\}}$, integrated along the vertical scattering vector $q_{z}$ of the Bragg rod, varies in the range 2.3-4.7. These results are incompatible with the GID measurements: the $\{0,1\}$ reflection was not observed (Table 2), and the intensity of the $\{1,1\}+\{1, \overline{1}\}$ reflection is strong (Figures 1 and 3 ). Thus we dismiss the two plane groups $p 11 g$ and $p 2 m g$. For the plane groups $p 1 g 1$ and $c 1$, the molecules were given a full rotation in $\phi$ about their chain axes, so as to generate all feasible packing arrangements. The results of the structure-factor

[^4] derived for the 2D crystal structure of arachidamide monolayers. ${ }^{34}$

## Scheme 1



Table 2. Observed and Calculated GID Data of the Monolayer of $\mathrm{C}_{31} \mathrm{H}_{63} \mathrm{OH}^{a}$

| $h k$ | $d(\mathbf{A})$ | $q_{x y}\left(\AA^{-1}\right)$ | $I_{0}$ | $I_{\text {c }}$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | plg1 | c1m1 | p11g | p2mg | c1 | model I | model II |
| \{0,1\} | 7.54 | 0.83 | $<3^{b}$ | c | $c$ | 100 | 100 | c | 0.1 | 8.1 |
| $\{0,2\}$ | 3.77 | 1.67 | 29.5 | 35.5 | 15.7 | 9.1 | 6.0 | 30.3 | 34.3 | 32.1 |
| $\{0,3\}$ | 2.51 | 2.50 | $<3{ }^{6}$ |  | c | 1.1 | 0.2 | c | 0.1 | 0.4 |
| $\{1,2\}+\{1,2\}$ | 3.01 | 2.09 | $<3^{\text {b }}$ | 1.9 | c | 4.3 | 4.7 | $c$ | 1.8 | 3.0 |
| $\{1,1\}+\{1,1\}$ | 4.16 | 1.51 | 100 | 100 | 100 | 25.1 | 31.6 | 100 | 100 | 100 |
| $\{1,0\}$ | 4.99 | 1.26 | <3 | 0.1 | $c$ | c | c | $c$ | 0.3 | 0.7 |
| \{2,0\} | 2.49 | 2.54 | 4.2 | 5.2 | 7.3 | 3.4 | 4.7 | 6.0 | 4.5 | 4.7 |

${ }^{6}$ Included are the observed ( $I_{0}$ ) and calculated ( $I_{c}$ ) intensities of the Bragg peaks for the various model structures on a relative scale. The intensities were calculated with molecular tilt angle $t=10^{\circ}$ and a rotation angle about the molecular axis $\phi=45^{\circ}$ for the plane groups $p 1 g 1, p 11 g$, and $c 1$. $q_{x y}$ $=4 \pi \sin \theta / \lambda$ is the horizontal scattering vector. Model $I$ is the pseudo $p 1 g 1$ glide model with an all-trans molecular conformation. Model II is the pseudo $p 1 \mathrm{~g} 1$ glide model in which the unit cell contains one molecule with the all-trans conformation and the other molecule with an end-of-chain $\mathrm{C}-\mathrm{OH}$ gauche conformation. ${ }^{b}$ These reflections were unobserved. Intensities estimated to be $<3 .{ }^{c}$ A symmetry forbidden reflection.
calculations pertaining to the three observed reflections were expressed in terms of the reliability fit indices $R=\Sigma\left|I_{0}-I_{\mathrm{c}}\right| / \Sigma I_{0}$ and $R_{w}=\sum w\left|I_{o}-I_{\mathrm{c}}\right| / \sum w I_{o}$, where $I_{\mathrm{o}}$ and $I_{\mathrm{c}}$ are the observed and calculated intensities of the individual points along the Bragg rod profile of the observed reflections and the weight $w$ is the inverse of the estimated standard deviation of $I_{0}$. The variation in $R_{\mathrm{w}}$ for the monolayers as a function of $\phi$ is significant (Figure 2a and b). From this curve and from comparison of the observed and calculated ratios of $I_{\{0,2\}}: I_{\{1.1\}+\{1.1\}}(0.295$ vs 0.157 , Table 2 ), we tend to dismiss the structure in plane group clm , which is a special case of $p 1 g 1$ when the angle of rotation of the molecular chain is at $\phi=90^{\circ}$ (see Scheme 1a).

The Bragg rod data does not allow us, however, to distinguish between plane groups $c 1$ and $p 1 g 1$, because the fit indices $R_{\mathrm{w}}$ for the two plane groups are almost the same for all values of the angle $\phi$ (Figure 2a). The minimum value of $R_{w}$ occurs for either of the structurally different orientations $\phi \approx 35^{\circ}$ and $215^{\circ}$ (as well as for their mirror images, $\phi \approx 145^{\circ}$ and $325^{\circ}$ ) shown in Figure $2 \mathrm{a}-\mathrm{c}$. Thus the Bragg rod data also do not allow us to distinguish between a particular structure and its $180^{\circ}$ rotational counterpart about the molecular axis. A calculated lattice energy profile as a function of the rotation angle $\phi$ provides complementary information to the results of the Bragg rod analysis. The
energy curve (Figure 2d) allows us to rule out plane group c1, the arrangement being less stable than $p 1 \mathrm{gl}$ by about $2 \mathrm{kcal} / \mathrm{mol}$ (or ca. 3 times the thermal energy, $R T \sim 0.6 \mathrm{kcal} / \mathrm{mol}$ ) at the minimum-energy arrangements corresponding to $\phi \approx 35^{\circ}$ and $215^{\circ}$. Moreover, the plane group cl is unlikely, because the packing arrangement of the chains with $\phi=35^{\circ}$ (Scheme 1e) does not involve any molecular symmetry element which would justify the observed rectangular cell. ${ }^{33}$ Finally, as mentioned earlier, the cell dimensions projected along the molecular chain, $a_{\mathrm{p}}=4.98 \AA$ and $b_{\mathrm{p}}=7.42 \AA$, are fingerprint evidence in favor of the orthogonal $\left(\mathrm{O}_{\perp}\right)$ motif in plane group $p 1 g 1$. But there is still one remaining ambiguity: the calculated energy difference of about $0.5 \mathrm{kcal} / \mathrm{mol}$ between the two minimum-energy states

[^5]

Figure 2. (a) Reliability index $R_{w}$ of the 2D crystal structure of $\mathrm{C}_{31} \mathrm{H}_{63} \mathrm{OH}$, as a function of rotation in $\phi$ of the molecule about its chain axis, for different molecular arrangements in different plane groups. The latter include $p 1 g 1, c 1 m 1$ (a special case of $p 1 g 1$ when $\phi=90^{\circ}$ ), and $c 1$. The curves for $p l g 1$ and $c 1$ almost coincide. (b) The same as in part a, for all three alcohol monolayers, but excluding plane group $c 1$. The $R_{w}$ index for plane group $c 1 m 1$ is indicated as well as the positions for which $R_{w}$ is minimum. Note that the crystal structures for $\phi=90^{\circ} \pm \Delta \phi$ and $270^{\circ} \pm \Delta \phi$ are identical. (c) Views along the molecular axis of the structures corresponding to various $\phi$ values, for the plane groups $p 1 g 1$ and $c 1$ (which both become $c 1 \mathrm{ml}$ for $\phi=90^{\circ}$ or $270^{\circ}$ ). The molecules have a tilt to the direction of the $b$ axis. (d) Calculated latice energy profiles of the $\mathrm{C}_{31} \mathrm{H}_{63} \mathrm{OH}$ monolayer crystallite as a function of rotation about $\phi$, the molecule with an all-trans conformation for the $c 1$ (dotted line) and $p 1 g 1$ (solid line) plane groups. The energy differences $\Delta E$ between the minima of the two plane groups are $1.4,1.2$, and $2.4 \mathrm{kcal} / \mathrm{mol}$ for the alcohol monolayers $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}, n=$ $23,30,31$, respectively. (e) The same as in part d, but for plane group $p 1 \mathrm{gl}$ only, for all the three alcohol monolayers. The minimum-energy positions at $\phi=35^{\circ}$ and $215^{\circ}$ are indicated. Note the labels $\mathrm{C}_{23} \mathrm{OH}, \mathrm{C}_{30} \mathrm{OH}$, and $\mathrm{C}_{31} \mathrm{OH}$ represent $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}, n=23,30,31$, respectively.
at $\phi \approx 35^{\circ}$ and $215^{\circ}$ in plane group $p 1 \mathrm{~g} 1$ (Figure 2e) is too low to pinpoint the actual structure.
3.2. Refinement of the 2D Crystal Structures using the GID Data. The fit of the calculated to the observed Bragg rod profiles for the three monolayers assuming plane group p1g1 is shown in Figure 3 (dashed line). There appears to be distinct room for improvement of the calculated Bragg rod profiles. We have assumed the molecules pack in plane group p1g1 of perfect symmetry. But is such an assumption justified for a monomolecular layer on the water surface? Thus we relaxed the glide symmetry of the crystal by tilting all the molecules by the same angle $\delta$ about an axis parallel to $b$ and which lies halfway between adjacent glide planes (Scheme 2). ${ }^{35}$

The pseudo glide model with values of the angle $\delta=1.2,1.7$, and $1.7^{\circ}$ for the alcohol monolayers $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}, n=23,30,31$, respectively, yielded, ${ }^{36}$ especially for the alcohols $n=30$ and 31, a distinct improvement in the reliability indices $R$ and $R_{w}$ (Table 3) and also in the Bragg rod fits as illustrated in Figure 3. The calculated lattice energies of these pseudo glide models differed by no more than $\pm 1 \mathrm{kcal} / \mathrm{mol}$ from those of the pure glide. Thus the deduced plane group is $p 1$ with two crystallographically independent molecules per unit cell (Figure 4). A similar relaxation in glide symmetry was deduced for the uncompressed monolayers of the carboxylic acid ${ }^{7} \mathrm{C}_{29} \mathrm{H}_{59} \mathrm{CO}_{2} \mathrm{H}$ over water at a temperature of about $5^{\circ} \mathrm{C}$. The hydrocarbon chains of the
(36) As in the case for the pure glide symmetry, the molecular orientation was optimized by rotating the molecule about the $\phi$ axis.
three alcohol monolayers are arranged in the orthogonal $\mathrm{O}_{\perp}$ motif with an average angle $\eta$ of $86^{\circ}$ (Table 3b) between the planes of the pseudo glide-related molecules (Figure 4). This angle is close in value to that found in the 3D crystal structure of the alcohol $\mathrm{C}_{24} \mathrm{H}_{49} \mathrm{OH}$ (see section 6.3).

The Bragg rod fitting was insensitive to variation in $U_{z}$, the molecular thermal vibrational factor along the $z$ direction, in the range $0.05-2 \AA^{2}$. This is because the molecules are aligned almost vertically, so that the intensity of the Bragg rods falls off rapidly at low $q_{z}$. Thus $U_{z}$ was arbitrarily set at a value of $0.5 \AA^{2}$. On the other hand, a reliable value for the inplane thermal vibrational parameter $U_{x y}$ for each alcohol monolayer could be extracted from the Bragg rod data, because the three observed reflections are distributed over a sufficiently large range in $q_{x y}$. Refinement yielded $U_{x y}$ values of $0.07,0.04$, and $0.08 \AA^{2}$ for the three alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}, n=23,30,31$, respectively, as shown in Figure 5 for $n=30,31$. The average value of $0.07 \AA^{2}$ is in the same range as that obtained for the hydrocarbon chains in the 3D crystal structures of $N$-(2-hydroxyethyl)octadecanamide ${ }^{37}\left(\mathrm{CH}_{3}\left(\mathrm{CH}_{2}\right)_{16^{-}}\right.$ $\left.\mathrm{CONH}\left(\mathrm{CH}_{2}\right)_{2} \mathrm{OH}\right)$ and $n$-hexatriacontane ${ }^{38}\left(n-\mathrm{C}_{36} \mathrm{H}_{74}\right)$ at room temperature.
The structure refinement of the three alcohol monolayers does allow us to extract a reliable measure of their relative amounts of crystalline material on the water surface because the GID

[^6]

Figure 3. Observed and calculated Bragg rods of the $\{1,1\}+\{1, \overline{1}\},\{0,2\}$, and $\{2,0\}$ reflections of the alcohol monolayers $\left(\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}, n=23,30\right.$, 31), assuming an all-trans molecular conformation and $p 1 g 1$ (dotted line) and pseudo p1g1 (solid line) plane symmetry.

## Scheme 2


measurements were made under similar experimental conditions. We make use of the equation $I^{\mathrm{c}}{ }_{h k}\left(q_{z}\right)=K I^{\circ}{ }_{h k}\left(q_{z}\right)$, where $I^{c_{k k}}\left(q_{z}\right)$ the calculated Bragg rod intensity derived from eq 1, is scaled to the observed value $I^{\circ}{ }_{k k}\left(q_{z}\right)$ by the factor $K$. The derived values of $1 / K$ for the three monolayers $(1,0.79,0.99$ for $n=23,30,31$, respectively) provide a measure of their relative amounts of crystallinity. ${ }^{39}$
3.3. Analysis of the Head-Group Conformation. Here we shall review the various structural characteristics of 3D crystal structures of alcohols and diols in connection with the conformational and packing properties of the alcohol monolayers. Molecules of the alcohol $n-\mathrm{C}_{24} \mathrm{H}_{49} \mathrm{OH}$ adopt an all-trans conformation in the solid state and are interlinked at one end by an $\mathrm{O}-\mathrm{H} . . . \mathrm{O}$ hydrogen bond (Figure 6). This is also true for the molecules of the diol $\mathrm{HO}\left(\mathrm{CH}_{2}\right)_{10} \mathrm{OH}$, which are interlinked at both ends by hydrogen bonds (Figure 7). The molecules are respectively tilted at an angle of $36^{\circ}$ and $46^{\circ}$ from the normal to the layer. By comparison, in the 3D crystal structure ${ }^{8.11}$ of $\mathrm{C}_{17} \mathrm{H}_{35} \mathrm{OH}$, every other molecule exhibits a gauche conformation of the $\mathrm{C}_{\alpha}-\mathrm{OH}$ group about the $\mathrm{C}_{\beta}-\mathrm{C}_{\alpha}$ bond, and in the crystal structure of $\mathrm{HO}\left(\mathrm{CH}_{2}\right)_{9} \mathrm{OH}$ (Figure 8), one end of each molecule adopts a $\mathrm{C}_{\alpha}-\mathrm{OH}$ gauche conformation about the $\mathrm{C}_{\beta}-\mathrm{C}_{\alpha}$ bond. In these two latter crystal structures the molecules are aligned vertically with respect to the layer plane. They form both intraand interlayer $\mathrm{O}-\mathrm{H} \ldots \mathrm{O}$ hydrogen bonds between molecules of unlike end-of-chain gauche and trans $\mathrm{C}-\mathrm{OH}$ conformations.

In view of the fact that the chains of $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}(n=23,30$, 31) in the monolayers are tilted from the vertical by an angle as

Table 3. Results of the Bragg Rod Fitting and Packing Energy Calculations for the Alcohol $\left(\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}, n=23,30,31\right)$ Monolayers ${ }^{a}$

|  | $\mathrm{C}_{23} \mathrm{H}_{47} \mathrm{OH}$ | $\mathrm{C}_{30} \mathrm{H}_{61} \mathrm{OH}$ | $\mathrm{C}_{31} \mathrm{H}_{63} \mathrm{OH}$ |
| :---: | :---: | :---: | :---: |
| (a) All-trans Molecular Conformation in the Crystal with Pure plgl Glide Symmetry |  |  |  |
| $t$ (deg) | 9.4 | 7.8 | 9.7 |
| tilt | 9.4 | 7.8 | 9.7 |
| $\eta$ (deg) | 107.0 | 112.8 | 113.6 |
| $\boldsymbol{R}$ | 0.31 | 0.40 | 0.36 |
| $\boldsymbol{R}_{\text {w }}$ | 0.41 | 0.49 | 0.46 |
| $E(\mathrm{kcal} / \mathrm{mol})$ | -48.1 | -63.3 | -66.1 |
| $E^{\prime}(\mathrm{kcal} / \mathrm{mol})$ | -47.7 | -63.0 | -65.7 |
| (b) All-trans Molecular Conformation with Pseudo $p 1 \mathrm{~g} 1$ Glide Symmetry |  |  |  |
| $\delta$ (deg) | 1.2 | 1.7 | 1.7 |
| $t$ (deg) | 9.3 | 8.0 | 9.8 |
| tilt | 9.3 | 8.0 | 9.8 |
| $\eta$ (deg) | 90.0 | 86.0 | 82.0 |
| $\boldsymbol{R}$ | 0.30 | 0.34 | 0.28 |
| $\boldsymbol{R}_{\mathbf{w}}$ | 0.40 | 0.42 | 0.38 |
| $E(\mathrm{kcal} / \mathrm{mol})$ | -48.2 | -64.1 | -65.7 |
| $E^{\prime}(\mathrm{kcal} / \mathrm{mol})$ | -47.4 | -63.4 | -64.7 |

(c) As in Part b, but with $50 \%$ of the Molecules Having a Gauche $\mathrm{C}_{\alpha}-\mathrm{OH}$ Conformation

| $\delta(\mathrm{deg})$ | 1.1 | 1.7 |  |
| :--- | :--- | :--- | :--- |
| $t(\mathrm{deg})$ | 9.6 | 7.9 | 1.6 |
| $t i l t(\mathrm{deg})$ | 9.7 | 8.1 | 9.9 |
| $\eta(\mathrm{deg})$ | 84.0 | 84.0 | 10.0 |
| $R$ | 0.30 | 0.34 | 88.0 |
| $R_{w}$ | 0.40 | 0.42 | 0.28 |
| $E(\mathrm{kcal} / \mathrm{mol})$ | -47.2 | -62.7 | 0.38 |
| $E^{\prime}(\mathrm{kcal} / \mathrm{mol})$ | -47.0 | -62.1 | -64.7 |

$a_{t}=$ angle of tilt of the molecular chain from the vertical to the direction of the $b$ axis. ${ }^{23} \delta=$ angle of distortion of the glide plane as defined in Scheme 2. tilt $=$ total tilt angle of the molecular chain from the vertical. ${ }^{35}$ $\eta=$ Dihedral angle between the molecular planes of two molecules related by (pseudo) glide symmetry, subtended along the $a$ axis; so $\eta=180^{\circ}$ $2 \phi$, where $\phi$ is defined in the text. $R$ and $R_{\mathrm{w}}$ are the fit indices: $R=$ $\Sigma\left|I_{0}-I_{\mathrm{c}} / \sum I_{0} ; R_{w}=\sum w\right| I_{0}-I_{\mathrm{c}} \mid / \sum w I_{o} . E=$ the crystal lattice energy corresponding to the minimum $R_{w}$ value. $E^{\prime}=$ the crystal lattice energy with the molecule rotated by $180^{\circ}$ about its chain axis.
low as $9^{\circ}$, it was necessary to examine whether these molecules do not adopt a layer arrangement akin to that of $\mathrm{C}_{17} \mathrm{H}_{35} \mathrm{OH}$ or $\mathrm{HO}\left(\mathrm{CH}_{2}\right), \mathrm{OH}$. Thus we constructed analogous arrangements for the three alcohol monolayers by inserting a $\mathrm{C}-\mathrm{OH}$ gauche conformation for the molecule in the center of each unit cell, as shown in Figure 9. There was little change in the calculated intensity profiles of the Bragg rods of the three observed reflections, although the model yields a weak calculated $\{0,1\}$ reflection, which was not observed (Table 2). The calculated lattice energies of these models are about $1 \mathrm{kcal} / \mathrm{mol}$ less stable than those of the corresponding structures with all-trans conformations (Table 3c). This energy difference is in addition to a higher intramolecular energy, of $0.4 \mathrm{kcal} / \mathrm{mol}$, of the gauche conformer, according to a calculation using published molecular force field parameters. ${ }^{40}$
The monolayer structures with the gauche-trans molecular model suffer from two drawbacks, as reflected in the higher lattice energy vis-a-vis the all-trans molecular model. One involves the poor intermolecular contacts between methyl groups at the exposed surface of the monolayer, because the methyl groups of molecules with all-trans and end-of-chain gauche conformers differ in height by about $1.2 \AA$ (Figure 9a). This inherent disadvantage does not come into play in the 3D crystal structure of $\mathrm{C}_{17} \mathrm{H}_{35} \mathrm{OH}$, because of the presence of van der Waals interlayer contacts. The other drawback involves contacts at the hydroxyl end of the molecule. As we observe in Figure 9b, the arrangement does contain a favorable $\mathrm{O}-\mathrm{H} \ldots \mathrm{O}$ hydrogen bond (labeled $d_{1}$ ) of length $2.9 \AA$

[^7]

Figure 4. Structure of the alcohol monolayers $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}(n=23,30$, 31) in pseudo p1g1 symmetry. The angle of distortion of the pseudo glide plane $\delta=1.2^{\circ}, 1.7^{\circ}, 1.7^{\circ}$; the tilt angles $t$ to the direction of the $b$ axis are $9.2^{\circ}, 7.8^{\circ}, 9.7^{\circ}$; the dihedral angles $\eta=180^{\circ}-2 \phi$ are 90,86 , $82^{\circ}$ for $n=23,30,31$, respectively; the $\mathrm{O} \ldots \mathrm{O}$ distances between pseudo glide related molecules in the unit cell are $d_{1}=4.2 \AA, d_{2}=4.8 \AA$ for all three monolayers: (a) view along the $b$ axis; (b) view along the $a$ axis; (c) view along the molecular chain axis. Note that $a_{\mathrm{p}}$ and $b_{\mathrm{p}}$ represent the unit cell $a$ and $b$ axes projected onto a plane perpendicular to the molecular chain axis.
between the gauche and trans conformers related by the pseudo glide. But the arrangement also contains a non-hydrogen-bonded contact between oxygen atoms (labeled $d_{2}$ ) of $3.4 \AA$. This contact is made through the lone-pair electrons of the two oxygen atoms and is thus weakly repulsive. ${ }^{41}$ We may avoid this weakly repulsive interaction by an appropriate rotation of the OH bond of the molecule with the end-of-chain trans conformer, as shown in Figure 9c. Alternatively, the repulsive $\mathrm{O} \ldots \mathrm{O}$ contact in Figure 9 b may be averted by adopting the alternative gauche conformation shown in Figure 9d. But the O-H...O distance ( $d_{1}$ ) would be too long at $3.4 \AA$ for a hydrogen bond. Surprisingly an analogous arrangement is found in the hydrogen-bonding layer structure of $\mathrm{HO}\left(\mathrm{CH}_{2}\right)_{9} \mathrm{OH}$, but here the $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ distance is $2.74 \AA$, suitable for hydrogen bonding (Figure 8). This is made possible because the $a$ axis, which is parallel to the $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ bond, is $6.88 \AA$ (Table 4a), namely $0.6 \AA$ shorter than the corresponding $b$ axis of the monolayer structures. Nevertheless, these 2D structures have a serious drawback when we consider interaction with the underlying solvent water molecules. When a water molecule makes simultaneous hydrogen bonds with two neighboring OH groups, the distance between these two oxygen atoms is in the range $4.6 \AA$ (Scheme 3). The monolayer packing arrangement with the all-trans conformation is ideally suited for such a condition because the distances between the oxygen atoms are 4.2 and $4.8 \AA$ and the lattice translation is $5.0 \AA$ (Figure 4). The arrangement of oxygen atoms in the trans-gauche model (Figure $9 \mathrm{~b}, \mathrm{c}$ ), contains $\mathrm{O} \ldots \mathrm{O}$ distances of $2.9,3.3$, and $5.0 \AA$,

[^8]

Figure 5. Observed Bragg rod intensity profiles of the $\{1,1\}+\{1, \overline{1}\},\{0,2\}$, and $\{2,0\}$ reflections of the $\mathrm{C}_{30} \mathrm{H}_{61} \mathrm{OH}$ and $\mathrm{C}_{31} \mathrm{H}_{63} \mathrm{OH}$ monolayers and the variation in the calculated profiles as a function of the in-plane temperature parameter $U_{x y}$. This parameter was given five values ranging from 0.01 to $1.00 \AA^{2}$ for each monolayer. The symmetry of the plane group is pseudo plg1. The temperature parameter $U_{z}$, along the vertical axis, was set at $U_{z}=0.5 \AA^{2}$.


Flgure 6. Packing arrangement of 1-tetracosanol ( $\mathrm{C}_{24} \mathrm{H}_{4} \mathrm{OH}$ ), showing contacts between methyl groups and between hydroxy groups (for convenience, only part of the chains of the top and bottom layers is shown). Note the disordered locations of the hydroxyl H atoms bonded to the O atoms ( O ). But within any hydrogen-bonding chain, the hydroxyl H atoms cannot be disordered, as shown in the insert. Thus, two different hydrogen-bonding chains, corresponding to each of two disordered H locations, coexist in the crystal.
which would be less satisfactory for hydrogen bonding to a layer of water molecules.



Figure 7. (Top) Molecular structure of 1,10 -decanediol. (Bottom) Stereoscopic view of the molecular packing arrangement, showing interlayer hydrogen bonding.




Figure 8. (Top) Molecular structure of 1,9-nonanediol. (Middle) Stereoscopic view along the $b$ axis of the molecular packing arrangement, showing intralayer hydrogen bonding. (Bottom) Stereoscopic view along the $a$ axis of the molecular packing arrangement, showing intra- and interlayer hydrogen bonding.

Supporting evidence for the preference of the all-trans molecular model also comes from the ice-nucleation experiments, involving monolayers of the long-chain alcohols which, when spread on drops of water, act as efficient ice nucleators. ${ }^{1,13}$ There is certainly a better structural match between the arrangement of alcohol OH groups for the all-trans conformers than for the mixed alltrans and $\mathrm{C}-\mathrm{OH}$ gauche conformers, as is evident from Figure 10. This observation is in good agreement with the fact that the crystals of $\mathrm{HO}\left(\mathrm{CH}_{2}\right), \mathrm{OH}$, whose hydrogen-bonding layer structure (Figure 8) contains a mixture of trans and gauche end groups, proved to be very poor ice nucleator. Drops of water deposited upon the hydrophilic (010) face of plate-like crystals of HO$\left(\mathrm{CH}_{2}\right)_{9} \mathrm{OH}$ froze only upon cooling the crystals down to a temperature as low as $-15^{\circ} \mathrm{C} 1^{13}$ On the basis of all this evidence, we may dismiss the mixed all-trans and $\mathrm{C}-\mathrm{OH}$ gauche model.

The ice-nucleation experiments may also be invoked to resolve the ambiguity discussed in section 3.1 regarding the azimuthal orientation of the molecules about their chain axes, as expressed


Figure 9. Possible molecular packing arrangements of alcohol monolayers ( $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}, n=23,30,31$ ) with half the number of molecules with their $\mathrm{C}_{\alpha}-\mathrm{OH}$ groups in the gauche conformation about the $\mathrm{C}_{\boldsymbol{\beta}}-\mathrm{C}_{\alpha}$ bond: (a) view along the $b$ axis showing the poor molecular contact between the methyl groups at the top of the monolayer; (b) view along the molecular axis, showing different $\mathrm{O} \ldots \mathrm{O}$ distances $d_{1}$ and $d_{2}$, which are of lengths 2.9 and $3.3 \AA$, respectively, for all three monolayers; (c) the same as in part b , but the $\mathrm{O}-\mathrm{H}$ bond of the all-trans conformer has been adjusted so as to form a long $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ contact with the oxygen atom of the gauche conformer; (d) packing arrangement with the alternative $\mathrm{C}_{\mathrm{\alpha}}-\mathrm{OH}$ gauche conformation, yielding $\mathrm{O} \cdots \mathrm{O}$ contacts almost parallel to the long $b$ axis. The two different $\mathrm{O} \cdots \mathrm{O}$ distances are $d_{1}=3.4 \AA$ and $d_{2}=4.5 \AA$ for all three monolayers.
in terms of the angle $\phi$. The lattice energy calculations indicate that the 2D arrangements of $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}(n=30,31)$ are the same from the hydroxyl head group up along the chain, so that a difference between the crystal structures of $n=30$ and 31 manifests itself in the position of the terminal methyl group. But the energy difference between the two orientational states $\phi=$ $35^{\circ}$ and $215^{\circ}$ is as low as $0.5 \mathrm{kcal} / \mathrm{mol}$. The ice-nucleation experiments do not yield information as to the absolute orientation of the molecular chains. But we interpret the differences in freezing point induced by the odd and even series as indicating that the positions of the OH groups of the $n$ even and odd series are different and subsequently that the azimuthal orientations of the chains of the $n$ odd and $n$ even series should not differ in $\phi$. Thus, if we assume, on the basis of the best fit of the observed and calculated Bragg rod intensity profiles, that $\phi=229^{\circ}$ for the structure of the monolayer of $\mathrm{C}_{31} \mathrm{H}_{63} \mathrm{OH}$, as shown in Figure 11, then $\phi$ is the same for the crystal structure of $\mathrm{C}_{30} \mathrm{H}_{61} \mathrm{OH}$.

## 4. Results on Monolayers of the $\mathrm{C}_{\mu} \mathrm{H}_{2 \mu+1} \mathrm{CO}_{2} \mathrm{C}_{\mu} \mathrm{H}_{2 \mu} \mathrm{OH}$ Series

4.1. Determination of the 2D Crystal Structures using the GID Data. The GID measurements are described in section 6.1. Two distinct Bragg peaks were observed, for each of the two monolayers, HDE and HNE. These Bragg peaks with their corresponding Bragg rods are shown in Figure 12. The crystallite coherence lengths $L$ derived from the widths of the Bragg reflections, ${ }^{42}$ are anisotropic, $>1000 \AA$ for the sharp reflection at $q_{x y}=1.68 \AA^{-1}$, and $\sim 450 \AA$ for the broader reflection at $q_{x y}$ $=1.38 \AA^{-1}$. Thus both monolayers self-aggregate with a high

[^9]Table 4. Data for the Diols $\mathrm{HO}\left(\mathrm{CH}_{2}\right)_{n} \mathrm{OH}, n=9,10$ and Alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}, n=24,25$


## Scheme 3


degree of crystalline order. The GID patterns of the two monolayers are similar to each other and also to that obtained from the monolayer of triacontanoic acid ${ }^{7}$ at $5^{\circ} \mathrm{C}$, the structure of which had already been determined. Hence we could easily index the two reflections and so determine the unit cell dimensions and derive information such as plane symmetry and overall molecular packing characteristics. The two reflections at $q_{x y}=$ 1.38 and $1.68 \AA^{-1}$ were indexed as $\{1,1\}+\{1, \overline{1}\}$ and $\{0,2\}$, respectively, for a primitive rectangular cell, yielding the cell parameters listed in Table 5. The peak positions of the Bragg rod intensity profiles of the $\{0,2\}$ and $\{1, \overline{1}\}+\{1, \overline{1}\}$ reflections indicate that the molecules tilt at an angle $t$ of $\sim 29^{\circ}$ from the vertical in the direction of the short $a$ axis. ${ }^{43}$ The unit cell parameters of the $a b$ lattice projected onto a plane perpendicular to the molecular chain axis ( $a_{\mathrm{p}}, b_{\mathrm{p}}$ ) are also shown in Table 5. They are close to the values $a_{\mathrm{p}}=4.98 \AA, b_{\mathrm{p}}=7.42 \AA$, which is a fingerprint ${ }^{2.7}$ of hydrocarbon packing in the orthogonal $\mathrm{O}_{\perp}$ motif in plane group p11g for both monolayers HDE and HNE.

For the determination almost at the atomic level, of the 2D structures, we followed a procedure involving Bragg rod analysis and lattice energy calculations already described herein for the alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$.

Employing the X-ray structure factor eq 1, the intensity profiles of the Bragg rods corresponding to the two measured $\{1,1\}+\{1, \overline{1}\}$ and $\{0,2\}$ reflections were calculated using the atomic coordinate model. So as to generate all the possible arrangements with plane symmetry $p 11 \mathrm{~g}$, the molecules were given a full rotation in angle $\phi$ about their long-chain axes. The results were expressed in terms of the reliability fit indices $R$ and $R_{w}$. The variation in $R$ and $R_{w}$ as a function of $\phi$ was significant. The fit of the calculated
(43) Assuming that the aliphatic tails are uniformly and rigidly tilted in the monolayer, the angle $t$ between the molecular axis and the surface normal is given by $\cos \chi_{k k} \tan t=q_{z}^{\circ} /\left|q_{h k}\right|$, where $q_{z}^{\circ}$ is the position of the maximum along the Bragg rod and $\chi_{h k}$ is the azimuthal angle between the tilt direction projected on the $x y$ plane and the reciprocal lattice vector $q_{h k}$, as described in ref 16.

(c) $0^{\circ} 0^{\circ} 0^{\circ} 0^{\circ}$


$$
0^{0} 0^{0} 0^{0} 0^{0}
$$



Figure 10. Layer arrangements of the oxygen atoms in the following: (a) an (001) layer of hexagonal ice; (b) the alcohol $\left(\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}, n=\right.$ $23,30,31$ ) monolayers containing an all-trans conformation of the molecular chain; ( $c$ and $d$ ) the alcohol monolayers in which half the number of molecules adopt an end-of-chain gauche $\mathrm{C}_{\alpha}-\mathrm{OH}$ conformation about the $\mathrm{C}_{\beta}-\mathrm{C}_{\alpha}$ bond (cf. Figure 9). The ice lattice is depicted in terms of the regular hexagonal cell (solid line), $a_{\mathrm{H}}=b_{\mathrm{H}}=4.5 \AA, \gamma_{\mathrm{H}}=120^{\circ}$, and a centered rectangular cell (dotted line), $a_{\mathrm{R}}=a_{\mathrm{H}}+b_{\mathrm{H}}=4.5 \AA, b_{\mathrm{R}}$ $=b_{\mathrm{H}}-a_{\mathrm{H}}=7.79 \AA, \gamma_{\mathrm{R}}=90^{\circ}$. The regular rectangular lattice of the alcohol monolayers whose dimensions are given in Table 1 is drawn as well as a distorted hexagonal net joining the oxygen atoms.
to the observed Bragg rod profiles for the lowest value of the reliability index $R_{w}$ (Table 6a) is shown in Figure 13 (dotted line).
According to Figure 13 (dotted lines), there is room for improvement of the calculated Bragg rod profiles of HNE and HDE. We have assumed that the molecules pack in plane group $p 11 g$ of perfect symmetry. This assumption did not appear to be justified for other monolayers such as the carboxylic acid ${ }^{7}$ $\mathrm{C}_{29} \mathrm{H}_{59} \mathrm{CO}_{2} \mathrm{H}$ and the three alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$ described herein, where we had relaxed the glide symmetry of the crystal by tilting all the molecules by the same angle $\delta$ about an axis parallel to the glide direction and halfway between the adjacent glide planes.


Figure 11. Views along the $a$ axis (top) and the vertical $c$ axis (bottom) of the molecular packing arrangements of the alcohol monolayers $\mathrm{C}_{n} \mathrm{H}_{2 n+1}$ $\mathrm{OH}, n=30$ and 31 , in pseudo pl g 1 plane symmetry. The two molecules $n=30$ and 31 do not differ in orientation about their molecular axes. This is seen in the top figure. However, the situation in which both molecules are rotated in $\phi$ by $180^{\circ}$ is equally possible.


Figure 12. Observed Bragg diffraction peaks for $\{1,1\}+\{1, \overline{1}\}$ and $\{0,2\}$ reflections across the horizontal scattering vector $q_{x y}$ and their corresponding Bragg rod intensity profiles for the monolayers of $\mathrm{C}_{19} \mathrm{H}_{39}$ $\mathrm{CO}_{2} \mathrm{C}_{n} \mathrm{H}_{2 n} \mathrm{OH}, n=9$ and 10 , labeled HNE and HDE, respectively.

Table 5. Results of Bragg Peak Analysis for the Monolayers of HNE and HDE, i.e. $\mathrm{C}_{19} \mathrm{H}_{39} \mathrm{CO}_{2} \mathrm{C}_{n} \mathrm{H}_{2 n} \mathrm{OH}, n=9$ and 10 , respectively ${ }^{a}$

|  | $d_{11}(\AA)$ <br> compd <br> $L(\AA)$ | $d_{02}(\AA)$ <br> $L(\AA)$ | $a(\AA)$ <br> $\left(a_{\mathrm{p}}\right)$ | $b(\AA)$ <br> $\left(b_{\mathrm{p}}\right)$ | $\gamma$ <br> $(\mathrm{deg})$ | $A\left(\AA^{2}\right)$ <br> $\left(A_{\mathrm{p}}\right)$ | $t$ <br> $(\mathrm{deg})$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HNE | 4.57 | 3.75 | 5.76 | 7.50 | 90 | 21.60 | 30.0 |
|  | $\sim 450$ | $>1000$ | $(4.99)$ | $(7.50)$ |  | $(18.71)$ |  |
| HDE | 4.53 | 3.74 | 5.69 | 7.48 | 90 | 21.28 | 28.0 |
|  | $\sim 450$ | $>1000$ | $(5.02)$ | $(7.48)$ |  | $(18.77)$ |  |

${ }^{a}$ The symbols $t, L, a, b, a_{\mathrm{p}}, b_{\mathrm{p}}$, and $A$ are defined in Table 1 .
Thus we applied the same relaxation to the monolayers of HNE and HDE. Best fits were obtained for $\delta$ values of $1.5^{\circ}$ and $1.8^{\circ}$ for HNE and HDE, respectively. The reliability index $R_{\mathrm{w}}$ shows

Table 6. Results of the Bragg Rod Fitting and Packing Energy Calculations for the Monolayers of HNE and HDE ${ }^{a}$

|  | HNE | HDE |
| :---: | :---: | :---: |
| (a) Packing Model with Pure P11g Glide Symmetry |  |  |
| $t$ (deg) | 30 | 28 |
| $\eta$ (deg) | 72 | 84 |
| $\boldsymbol{R}$ | 0.29 | 0.30 |
| $\boldsymbol{R}_{\text {w }}$ | 0.37 | 0.39 |
| (b) Packing Model with Pseudo pl 1 g Glide Symmetry |  |  |
| $\delta$ (deg) | 1.5 | 1.8 |
| $t$ (deg) | 30 | 28 |
| $\eta$ (deg) | 88 | 98 |
| $\boldsymbol{R}$ | 0.25 | 0.24 |
| $R_{\text {w }}$ | 0.32 | 0.31 |

$a^{\prime} t=$ angle of tilt of the molecular chain from the vertical in the direction of the $a$ axis. The symbols $\delta, \eta, R$, and $R_{w}$ are defined in Table 3.


Figure 13. Observed and calculated Bragg rods of the $\{1,1\}+\{1, \overline{1}\}$ and $\{0,2\}$ reflections of HNE and HDE, assuming $p 1 g 1$ (dotted line) and pseudo plg1 (solid line) plane symmetry.


Figure 14. Reliability index $R_{w}$ of the 2D crystal structures of HNE and HDE, as a function of rotation in $\phi$ of the molecule about its chain axis. Note that the crystal structures about $\phi=90^{\circ}$ and $270^{\circ}$ are identical. The two different minima for HNE (dotted line), separated in $\phi$ by $180^{\circ}$, are the same, but for HDE (full line), the difference $\Delta R_{w} \approx 1 \%$.
$5-8 \%$ improvement (Table 6b) for the two structures, as manifested by the fits of the calculated Bragg rod intensity profiles illustrated in Figure 13 (solid line). For the pseudo glide model, the molecules were also given a full rotation about their chain axes. The variation in $R_{w}$ for the monolayers as a function of $\phi$ is significant, as shown in Figure 14. However, the Bragg rod data hardly allow one to distinguish between a structure and its $180^{\circ}$ rotational counterpart.

In these Bragg rod calculations, on the monolayers of HNE and HDE, we assumed a temperature factor of $1 \AA^{2}$ for $U_{2}$ and $0.1 \AA^{2}$ for $U_{x y}$. The value of $1 \AA^{2}$ for $U_{z}$ was taken from a GID analysis of tricontanoic acid over pure water, ${ }^{7}$ where the molecular tilt was about $30^{\circ}$ from the vertical. The value of $0.1 \AA^{2}$ was

(b)

## (a)

Figure 15. Observed Bragg rod intensity profiles of the $\{1,1\}+\{1, \overline{1}\}$ and $\{0,2\}$ reflections of HNE and HDE monolayers and the variation in the calculated profiles as a function of the out-of-plane ( $U_{z}$ ) and in-plane $\left(U_{x y}\right)$ temperature parameters. These parameters were each given five values ranging from 0.01 to $2.00 \AA^{2}$ for each monolayer; the solid line shows the best fit profile. The symmetry of the plane group is pseudo p11g. (a) variation in $U_{z}$, keeping $U_{x y}$ fixed at $0.1 \AA^{2}$; (b) variation in $U_{x y}$, keeping $U_{z}$ fixed at $1 \AA^{2}$.
taken from the analysis of the alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}, n=23,30$, 31 and from an analysis of the GID data of the monolayer of triacontanoic acid $\left(\mathrm{C}_{29} \mathrm{H}_{59} \mathrm{CO}_{2} \mathrm{H}\right)$ over $\mathrm{CdCl}_{2}$ solution at high $\mathrm{pH},{ }^{44}$ which yielded $U_{x y} \approx 0.08 \pm 0.03 \AA^{2}$, an estimate made possible by four observed Bragg rods spanning $q_{x y}$ in the range $1.54-1.84 \AA^{-1}$. The molecules in this 2D crystal structure are aligned almost vertical to the water surface. On the reasonable assumption that the in-plane $U_{x y}$ motion of HNE and HDE should be in the same range as that of the long-chain alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1}$ $\mathrm{OH}(n=30,31)$, we examined the effect of varying $U_{z}$ on the Bragg rod profiles but keeping $U_{x y}$ fixed at $0.1 \AA^{2}$. The results (Figure 15a) show that a good fit is obtained for a $U_{z}$ value of $1 \AA^{2}$. Limiting $U_{z}$ within the range of $0.5-1.0 \AA^{2}, U_{x y}$ was varied. A good fit was obtained for $U_{x y} \approx 0.1 \AA^{2}$ (Figure 15 b) but not when $U_{z}$ was set lower than $0.5 \AA^{2}$. Although it is obvious from Figure 15 that $U_{x y}$ and $U_{z}$ are strongly correlated, the derived values are reasonable on the basis of the measured data for the normal long-chain alcohols and acids.
4.2. Lattice Energy Calculations. As already mentioned, one ambiguity remains from the Bragg rod analysis of HNE and HDE (Figure 14); structures which differ only in axial rotation by $180^{\circ}$ give the same reliability index $R_{\mathrm{w}}$. To help overcome this ambiguity, lattice energy calculations were performed on the same ensemble of crystal structures as generated for the Bragg rod analysis. For convenience, we assumed that the structure is arranged in the perfect plane symmetry $p 11 g$.

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Figure 16. (a) Calculated lattice energy profiles of the monolayer crystallites of HNE and HDE (i.e. $\mathrm{C}_{19} \mathrm{H}_{39} \mathrm{CO}_{2} \mathrm{H}_{2 n} \mathrm{OH}, n=9,10$, respectively) as a function of rotation about $\phi$. Note the pure $p 11 \mathrm{~g}$ glide symmetry is assumed. The energy differences $\Delta E$ between the minima of the two monolayers are 1.2 and $3.6 \mathrm{kcal} / \mathrm{mol}$ for HNE and HDE, respectively. (b) The same as in part a, but for the NE and DE (i.e. $\mathrm{C}_{19} \mathrm{H}_{39} \mathrm{CO}_{2} \mathrm{C}_{n} \mathrm{H}_{2 n} \mathrm{H}, n=9,10$, respectively) models. $\Delta E$ values between the minima of the two monolayers are 2.6 and $2.5 \mathrm{kcal} / \mathrm{mol}$ for NE and DE, respectively.

The lattice energy profiles for HNE and HDE are shown in Figure 16a. The two energy minima for both HNE and HDE located at $\phi=54^{\circ}$ and $234^{\circ}$ differ by $\Delta E=1.2 \mathrm{kcal} / \mathrm{mol}$ for HNE and $3.6 \mathrm{kcal} / \mathrm{mol}$ for HDE. For both systems the lower energy is at $\phi=54^{\circ}$. The energy profiles are plotted in Figure 16 b for the analogous molecules which bear no OH group, namely the alkyl esters of $n$-nonyl eicosanoate (NE) and $n$-decyl eicosanoate (DE). Their energy profiles follow the same pattern as those of HNE and HDE, but $\Delta E$ is $\sim 2.6 \mathrm{kcal} / \mathrm{mol}$ for both systems. There is no doubt that the contributions of the NE and DE moieties of HNE and HDE, respectively, favor the same molecular orientation, at $\phi=54^{\circ}$. The additional OH group has a modifying influence; nevertheless, the energy differences still point to the same orientation for both monolayers. Therefore it is possible to fix the correct molecular orientation for pseudo glide symmetry from the Bragg rod analysis shown in Figure 14, leading to $\phi=44^{\circ}$ and $49^{\circ}$ for HNE and HDE, respectively. Their packing arrangements are shown in Figure 17
4.3. Correlation between Crystalline Coherence Length and Energy of Attachment. There is a pronounced difference in the crystal coherence length $L$ associated with the $\{1,1\}+\{1, \overline{1}\}$ and $\{0,2\}$ reflections of HNE and HDE (Table 5). $L$ is much smaller along the direction of molecular tilt. Triacontanoic acid ( $\mathrm{C}_{29} \mathrm{H}_{59^{-}}$ COOH ) and other fatty acids over pure water ${ }^{7}$ were also shown to exhibit crystalline coherence lengths which were smaller along the molecular tilt direction. This anisotropy of triacontanoic acid was accounted for in terms of the difference in the attachment energy ( $E_{\text {att }}$ ) of different ( $h, k$ ) rows of molecules to the crystal, the logic being that the lower the attachment energy, the easier it is to disturb or disrupt the crystal about the ( $h, k$ ) line. This effect should be more pronounced in systems exhibiting molecules with large tilt angles. The results of the attachment energy calculations in the 2D crystals of HNE and HDE are listed in Table 7. The attachment energy in the $b$ direction, corresponding to the $\{0,2\}$ reflection, is about $3 \mathrm{kcal} / \mathrm{mol}$ stronger than the


Figure 17. Structures of monolayers of the hydroxyl alkyl esters of HNE and HDE in pseudo p 11 g symmetry. The angle of distortion of the pseudo glide plane $\delta=1.8^{\circ}$ and $1.5^{\circ}$; the tilt angle $t$ from the vertical to the direction of the $a$ axis $=30^{\circ}$ and $28^{\circ}$; and the dihedral angle $\eta$ $=2 \phi=88^{\circ}$ and $98^{\circ}$ for HNE and HDE, respectively. Views are along (a) the $a$ axis, (b) the $b$ axis, and (c) the molecular chain axis. Note that $a_{\mathrm{p}}$ and $b_{\mathrm{p}}$ represent the unit cell axes $a$ and $b$ projected onto a plane perpendicular to the molecular chain axis.

Table 7. Energy of Attachment ( $E_{\text {att }}$ ) per Molecule between the $\{h, k\}$ Molecular Layer and the Rest of the Monolayer Crystal of HNE and HDE and the Measured Coherence Lengths along These $\{h, k\}$ Directions

| compound | $\{h, k\}$ | $E_{\text {att }}(\mathrm{kcal} / \mathrm{mol})$ | $L(\AA)$ |
| :---: | :---: | :---: | ---: |
| HNE | $\{1,1\}$ | -20.4 | 430 |
|  | $\{0,2\}$ | -23.1 | $\geq 1000$ |
| HDE | $\{1,1\}$ | -22.0 | 450 |
|  | $\{0,2\}$ | -24.7 | $\geq 1000$ |

attachment energy in the $a^{*} \pm b^{*}$ direction, corresponding to the $\{1,1\}+\{1, \overline{1}\}$ reflections. This result indicates that the crystal is probably more fragile along the molecular tilt direction, in agreement with the results obtained for triacontanoic acid.

## 5. Conclusion

The 2D crystal structures of the uncompressed monolayers of the alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}(n=23,30,31)$ and $\mathrm{C}_{19} \mathrm{H}_{39}-$ $\mathrm{CO}_{2} \mathrm{C}_{n} \mathrm{H}_{2 n} \mathrm{OH}(n=9,10)$ over water at $5^{\circ} \mathrm{C}$ have been determined at almost atomic level from the grazing incidence X -ray diffraction (GID) data and lattice energy calculations. The molecules crystallize, packing in a rectangular cell in the orthogonal $\mathrm{O}_{\perp}$ motif with pseudo glide plane symmetry. It was possible to get an estimate of the molecular motion in the crystal. The Bragg rod analysis and the energy calculations support the all-trans conformation of the molecule. The analysis does not allow one to distinguish between the structure of the normal alcohols $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$ and that of its $180^{\circ}$ rotational counterpart about the molecular axis. Nevertheless, the structure determination provides concrete evidence as to the role of a lattice and structural match for induction of ice nucleation by the long-chain $\mathrm{C}_{n} \mathrm{H}_{2 n+1^{-}}$ OH alcohol monolayers ${ }^{1,13}$ through an epitaxial mechanism.


## TOP VIEW

Figure 18. Top and side views of the GID geometry. The footprint of the grazing incidence beam is delineated. The position-sensitive detector (PSD) has its axis along the vertical direction. Only the area $A B C D$ contributes to the measured scattering.

It was possible to determine the absolute orientation of the molecules of $\mathrm{C}_{19} \mathrm{H}_{39} \mathrm{CO}_{2} \mathrm{C}_{n} \mathrm{H}_{2 n} \mathrm{OH}(n=9,10)$ by the lattice energy calculations. The anisotropy of the crystalline coherence lengths in the different crystalline directions of these two systems could be correlated with the energy of binding molecules in these directions. The orientations of the OH group of the two molecules $n=9,10$ with respect to the water surface are decidedly different. We may correlate this difference with their different ability to nucleate ice. ${ }^{13}$

## 6. Experimental Section

6.1. Grazing Incidence Diffraction Measurements from the Alcohol Monolayers. The measurements on monolayers were carried out using the liquid surface diffractometer on the synchrotron X-ray beam line D4 at Hasylab, DESY, Hamburg. A sealed and thermostated Langmuir trough equipped with a Wilhelmy balance, allowing for surface pressure control of the film, was mounted on the diffractometer. The synchrotron radiation beam was monochromated to a wave length $\lambda=1.39$ $\AA$ by Bragg reflection from a $\mathrm{Ge}(111)$ crystal and, to maximize surface sensitivity, was adjusted to strike the monolayer surface at an incident angle $\alpha_{\mathrm{i}}=0.85 \alpha_{\mathrm{c}}$ (where $\alpha_{\mathrm{c}}=0.138^{\circ}$ is the critical angle for total external reflection). This limits the penetration depth of the beam to that of the evanescent wave, and the scattering due to the subphase is efficiently reduced. This permits a reliable measurement of the weak diffraction signal originating from the crystalline monolayer. ${ }^{16}$ The dimensions of the footprint (Figure 18) of the incoming X-ray beam on the liquid surface were 50 $\times 5 \mathrm{~mm}$.

Chloroform solutions of long-chain alcohol $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}$ ( $n=$ $23,30,31)$ and of the hydroxy alkyl eicosanoates $\mathrm{C}_{19} \mathrm{H}_{39}-$ $\mathrm{CO}_{2} \mathrm{C}_{n} \mathrm{H}_{2 n} \mathrm{OH}, n=9,10$, labeled HNE and HDE, respectively, were spread on the water surface in the trough with $\sim 75 \%$ surface coverage at room temperature. The GID data were measured for a water surface temperature of $5^{\circ} \mathrm{C}$. The collection of the diffracted radiation was made in two ways using a one-dimensional position-sensitive detector (PSD, Figure 18), which intercepted photons over a range $0.0 \leq q_{z} \leq 0.9 \AA^{-1}$, mounted vertically behind a horizontally collimating Soller slit, of resolution width $\Delta\left(q_{x y}\right)=0.007 \AA^{-1}$. The scattered intensity, measured by scanning different values of $q_{x y}$ and integrating over the whole $q_{z}$ window of the PSD, yields Bragg peaks. Simultaneously, the scattered intensity recorded in channels along the PSD but integrated over $q_{x y}$ across a peak produces $q_{z}$-resolved Bragg rod intensity profiles. Three reflections were measured for each of the three alcohol $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}(n=23,30,31)$ monolayers in the $q_{x y}$ range 1.3-2.6
$\AA^{-1}$, as described previously. ${ }^{2}$ Two reflections were found for the HDE and HNE monolayers in the $q_{x y}$ range $0.70-1.80 \AA^{-1}$.
6.2. Structure Determination of 3D Crystals of 1,9-Nonanediol and 1,10-Decanediol. The compounds 1,9 -nonanediol ( $\mathrm{HO}-$ $\left.\left(\mathrm{CH}_{2}\right)_{9} \mathrm{OH}\right)$ and 1,10 -decanediol $\left(\mathrm{HO}\left(\mathrm{CH}_{2}\right)_{10} \mathrm{OH}\right)$ with $98 \%$ purity were purchased from Aldrich Co. Thin ( 0.05 mm ) platelike crystals of these two compounds for X-ray diffraction measurements were grown from chloroform and methylene chloride solutions, respectively, by slow evaporation at room temperature. A Rigaku AFC5 diffractometer equipped with a Mo rotating anode X-ray source was used for the intensity data collection on specimen crystals cooled to a temperature of $\sim 100$ K . The crystal structures were solved by direct methods using the SHELX86 computer program. ${ }^{45}$ All the H atoms were located from electron density difference maps. Conventional structurefactor least-squares refinement was performed using the SHELX76 program, ${ }^{46}$ with anisotropic thermal parameters for C and O atoms and isotropic thermal parameters for H atoms. Details of crystal data, X-ray intensity measurements, and refinement are listed in Table 4. The final $x, y, z$ coordinates, thermal parameters, bond distances, bond angles, and torsional angles are available as supplementary material.

The molecular structures and packing arrangements are shown in Figures 7 and 8. The molecular chain of 1,9-nonanediol has an all-trans conformation but for one end of the molecule where the $\mathrm{C}_{\alpha}-\mathrm{OH}$ bond adopts a gauche conformation about the $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond (torsion angle $\mathrm{C}_{\gamma}-\mathrm{C}_{\beta}-\mathrm{C}_{\alpha}-\mathrm{O}=-63.3^{\circ}$ ). The molecules pack in layers with the chain axes perpendicular to the layer whose area per molecule is $17.5 \AA^{2}$. These chains form the orthogonal $\mathrm{O}_{\perp}$ motif ${ }^{4,6}$ by twofold screw symmetry. The trans and gauche $\mathrm{C}-\mathrm{C}-\mathrm{C}-\mathrm{OH}$ moieties are interlinked by $\mathrm{O}-\mathrm{H} \cdot . . \mathrm{O}$ hydrogen bonds both within and between layers (Figure 8). The intralayer $\mathrm{O}-\mathrm{H} \cdot \ldots \mathrm{O}$ distance is $2.74 \AA$, and the interlayer distance is 2.70 Å.

The molecule of 1,10 -decanediol in its crystal structure has an all-trans conformation. It forms a layer structure in the $a b$ plane by translation symmetry only (Figure 7). The molecular chains are tilted at an angle of $44.1^{\circ}$ from the $a b$ plane. The projection of the $a b$ unit cell onto a plane perpendicular to the chain axis is $a_{\mathrm{s}}=4.02 \AA, b_{\mathrm{s}}=4.53 \AA, \gamma_{\mathrm{s}}=70.0^{\circ}$. With a tilt angle of $44.1^{\circ}$, the hydroxylOH groups are properly oriented to form a hydrogenbonded chain by twofold screw symmetry along the $b$ axis, with an $\mathrm{OH} \cdots \mathrm{O}$ distance of $2.80 \AA$, and so interlink neighboring $a b$ molecular layers.
6.3. Crystal Structure Determination of 1-Tetracosanol. Compounds of 1-tetracosanol ( $\mathrm{C}_{24} \mathrm{H}_{49} \mathrm{OH}$ ) and 1-pentacosanol $\left(\mathrm{C}_{25} \mathrm{H}_{51} \mathrm{OH}\right)$ with purity of $99 \%$ and $98 \%$, respectively, were purchased from Sigma Co. Thin diamond-shaped plate single crystals of these two compounds were obtained from methylene chloride solution by slow evaporation at room temperature. The

[^11]X-ray reflections from a crystal cooled to a temperature of $\sim 100$ K were measured on a Rigaku AFC5 diffractometer equipped with a Cu rotating anode X -ray source. The low-temperature cell parameters of these two crystals are shown in Table 4a. Details of the intensity data collection are listed in Table 4 b .

The crystal structure determination and refinement of 1-tetracosanol were essentially straightforward, although $\{h k l\}$ reflections with $h$ indices higher than 99 were not measured, because of a computer software limitation. Thus the refinement was performed by adjusting the $U_{11}$ temperature factor of each C and O atom to be equal to the average value of its $U_{22}$ and $U_{33}$ terms. The methylene hydrogen atoms were introduced into their proper positions. A single peak appropriate for a position of the hydroxy hydrogen atom was located on an electron density difference map, but as discussed below, the hydroxyl hydrogen atom must be disordered. The structure was refined to an $R$ value of $11.8 \%$.

The crystal structure of 1 -tetracosanol is composed of molecular layers parallel to $b c$. In the layer, the molecules which have an all-trans conformation are tilted from the normal to the $b c$ layer by $36^{\circ}$. They pack in the orthogonal $O_{\perp}$ motif by glide symmetry with a dihedral angle $\eta$ of $87.7^{\circ}$ between the planes of the gliderelated molecules. Between the layers, the methyl groups of the molecules make $\mathrm{CH}_{3} \ldots \mathrm{CH}_{3}$ contacts of 3.87 and $3.95 \AA$ across centers of inversion and twofold screw axes, respectively. At the opposite end of the molecule, the hydroxyl oxygen atoms make contacts of $2.68 \AA$ across centers of inversion and $2.66 \AA$ across twofold axes. Thus the hydroxyl hydrogen atoms must occupy two disordered positions with half occupancy, yielding hydrogenbonded chains parallel to the $c$ axis, as shown in Figure 6.

The very long $c$ axis of the crystal of 1-pentacosanol $\left(\mathrm{C}_{25} \mathrm{H}_{51^{-}}\right.$ OH ) and the slightly warped shape of the specimen plate-like crystal made it very difficult to separate neighboring X-ray reflections. We were thus not able to refine the crystal structure to proper completion.

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Supplementary Material Available: Tables of the atomic coordinates, bond lengths, bond angles, and torsion angles of 3D crystalline 1,9-nonanediol, 1,10-decanediol, and 1-tetracosanol and the atomic coordinates of the 2D crystalline monolayers of $\mathrm{C}_{n} \mathrm{H}_{2 n+1} \mathrm{OH}(n=23,30,31)$ and $\mathrm{C}_{19} \mathrm{H}_{39} \mathrm{CO}_{2} \mathrm{C}_{n} \mathrm{H}_{2 n} \mathrm{OH}$ ( $n=$ 9,10 ) ( 35 pages). This material is contained in many libraries on microfiche, immediately follows this article in the microfilm version of the journal, and can be ordered from the ACS; see any current masthead page for ordering information.


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    \$ RISØ National Labortteryst
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